



Structural Pipe Design

Paul Imm, P.Eng. – Cambridge, Ontario, Canada

Riley Dvorak, P.E. – Maple Grove, MN

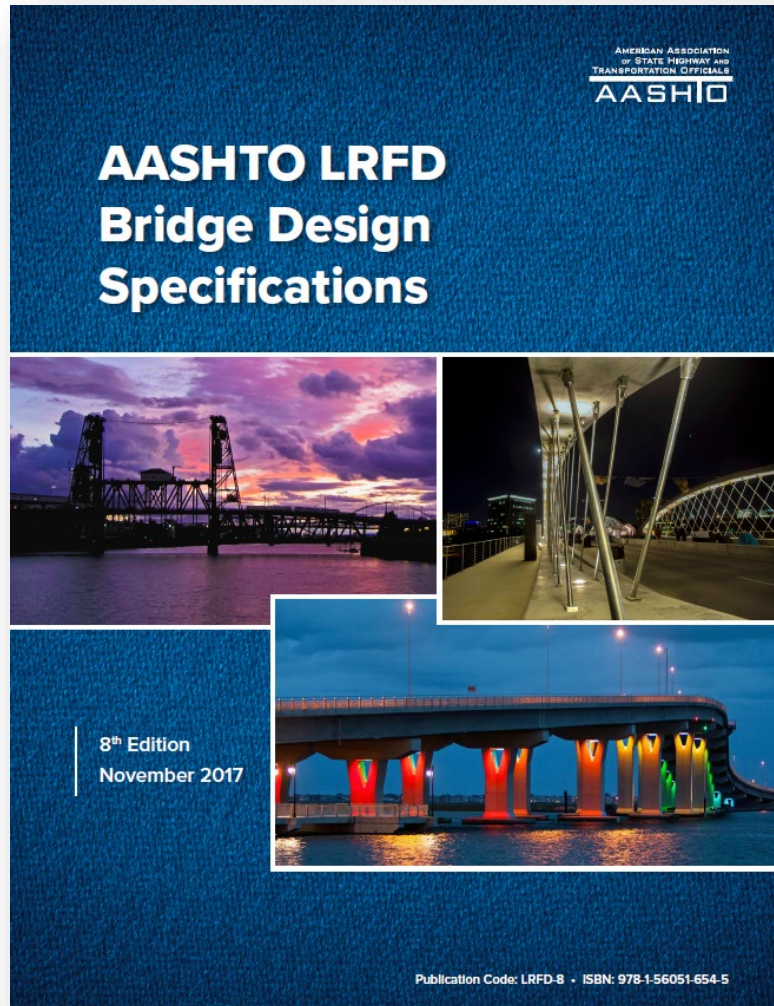


August 22, 2019

OVERVIEW

- Rigid vs flexible pipe behavior
- Design methods in AASHTO LRFD Section 12 Buried Structures:
 - Concrete pipe – Indirect Design with Standard Installations
 - Plastic pipe – Limit states design
- Summary

STRUCTURAL DESIGN OF BURIED PIPE



These structures become part of a composite system comprised of the pipe and the soil envelope.

12.10 – Reinforced Concrete Pipe

- Direct Design Method
- Indirect Design Method

12.12 – Thermoplastic Pipes

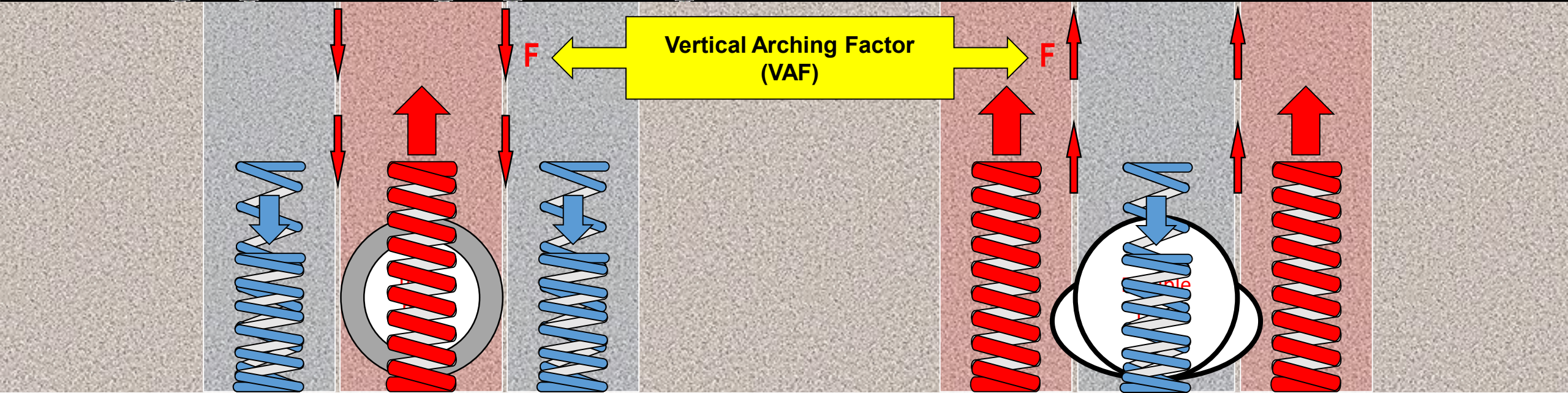
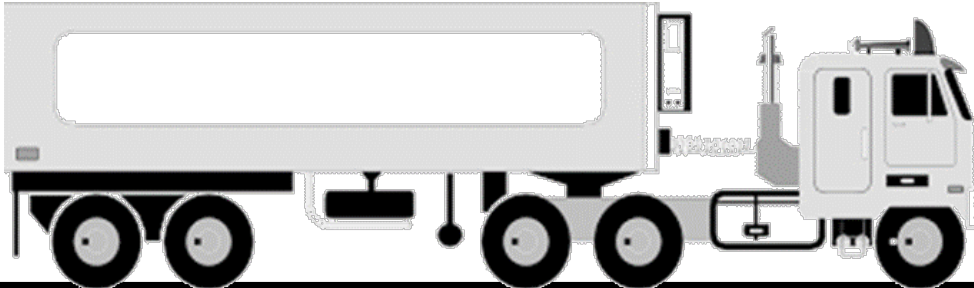
- Strength Limit States
- Service Limit States

ENGINEER OF RECORD RESPONSIBILITY

The professional engineer responsible for preparation of engineering drawings is also responsible for the structural design of pipe installations.

In all cases, designers shall keep a record of structural design calculations associated with each project. Design calculations for specific projects shall be provided to the City upon request.

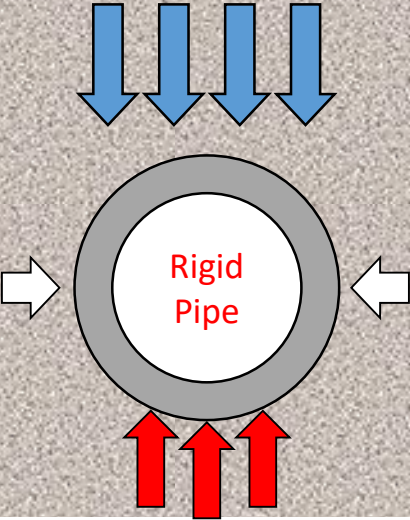
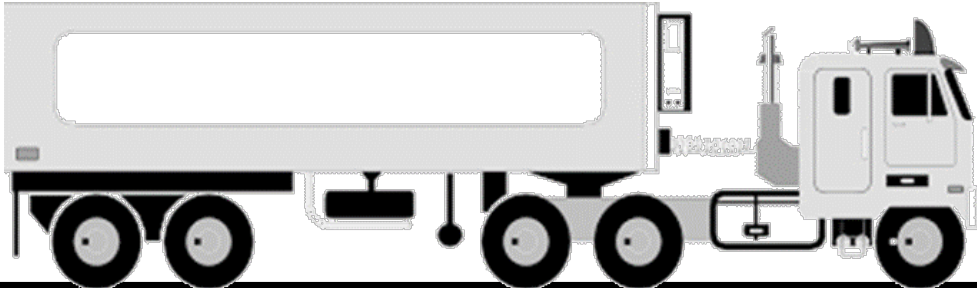
RIGID vs FLEXIBLE PIPE



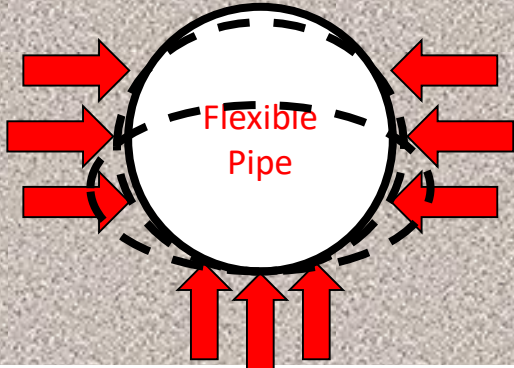
Rigid Pipe: $VAF > 1.0$
the pipe carries most of the load

Flexible Pipe: $VAF < 1.0$
embedment soil carries most of the load

RIGID vs FLEXIBLE PIPE



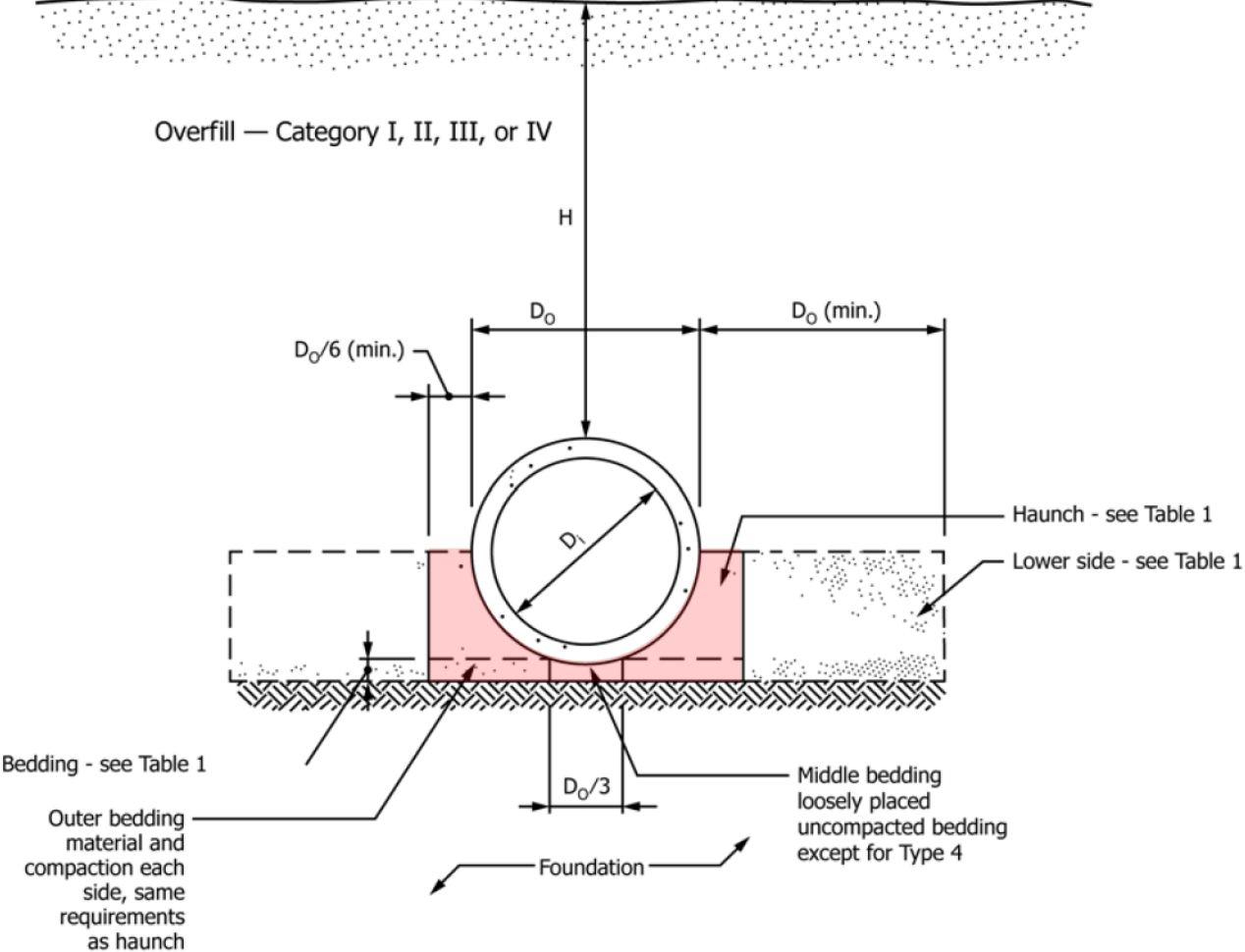
4 bedding types & 5 pipe classes
for economical design options



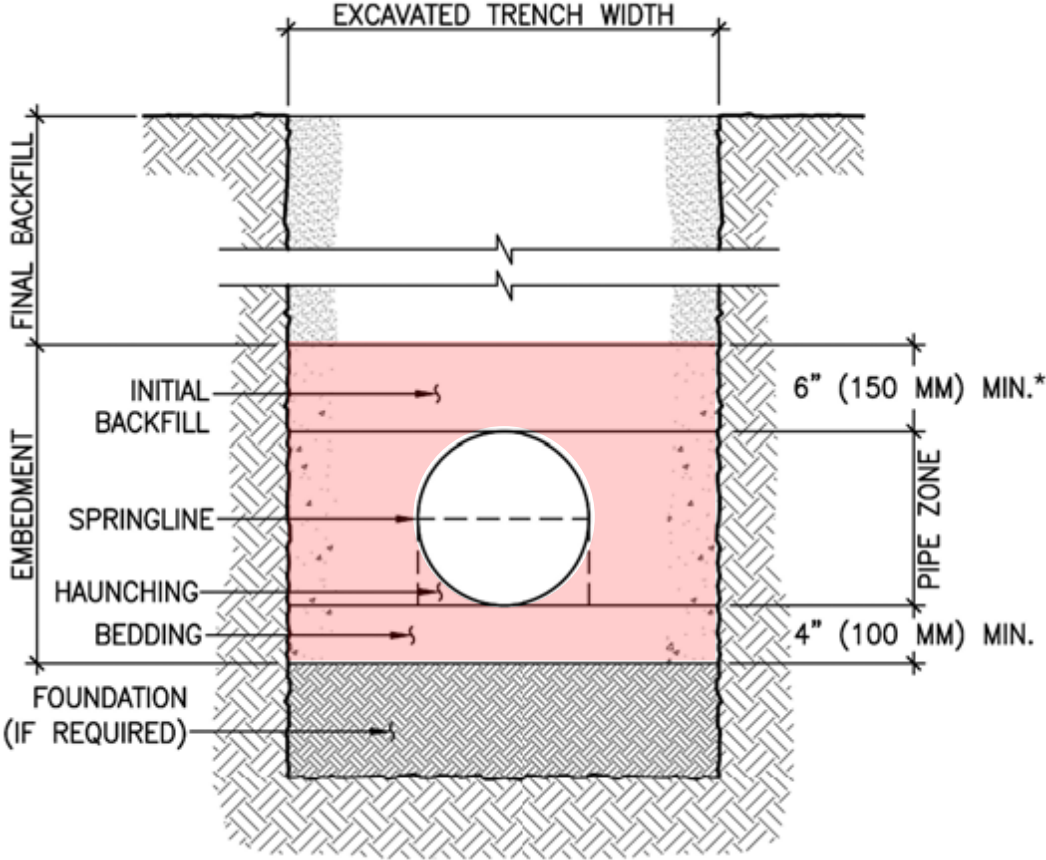
Passive side
soil support
to control
deflection

Installation sensitive and
complex design method

INSTALLATION DETAILS

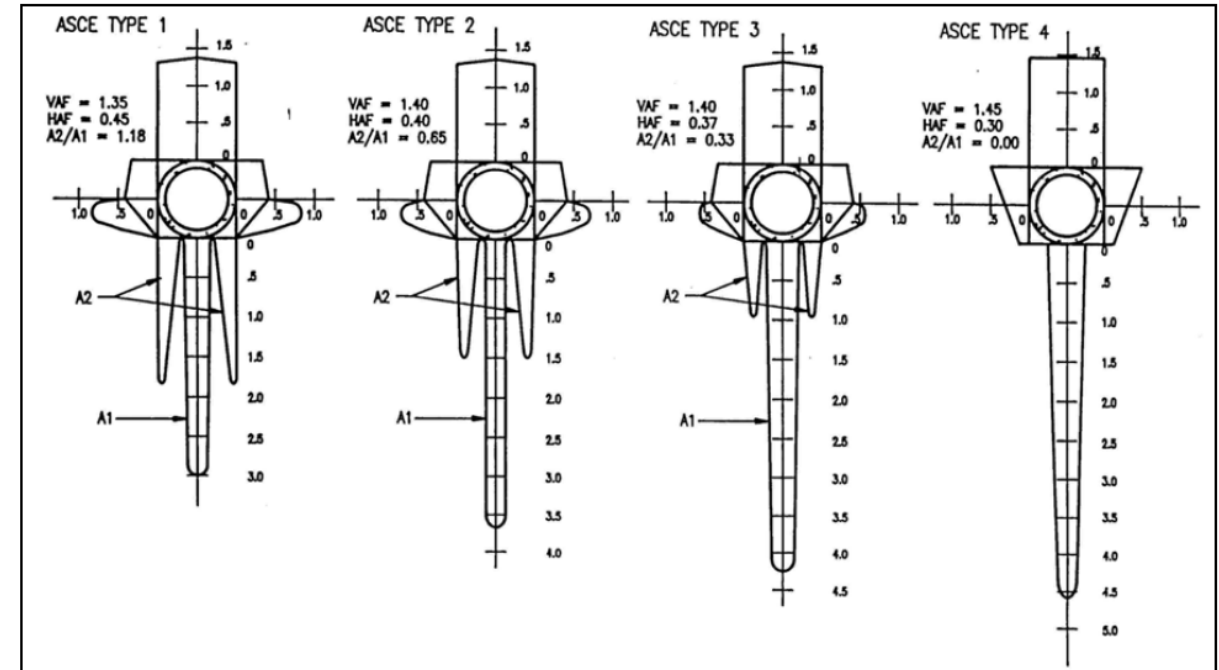
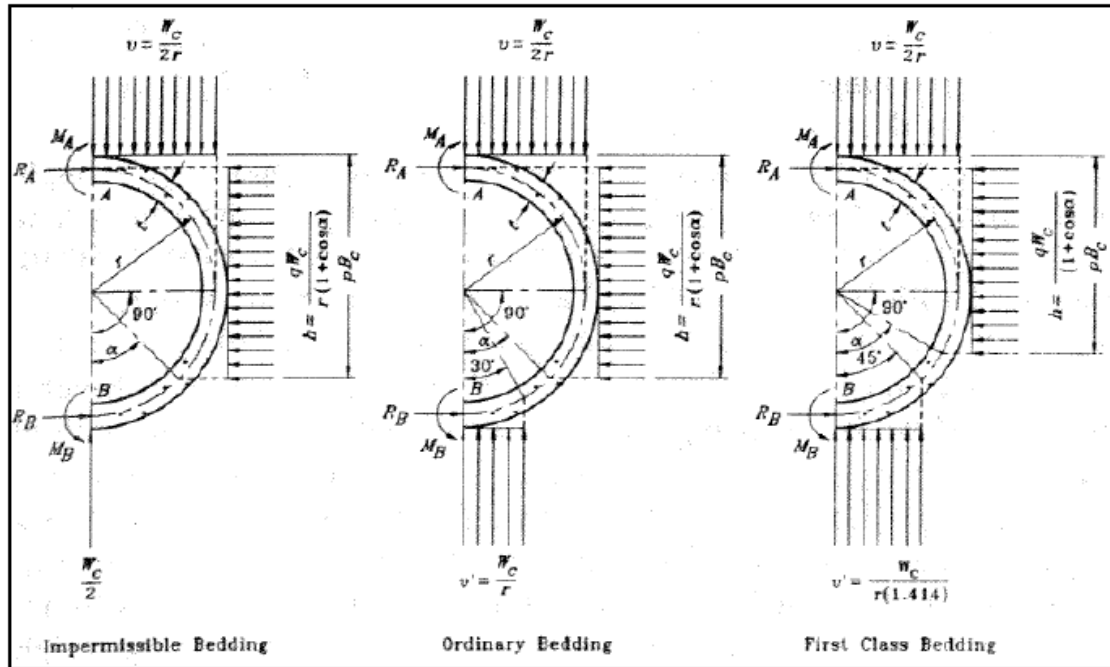


ASTM C1479 for Concrete Pipe



ASTM D2321 for Plastic Pipe

EVOLUTION OF RCP DESIGN



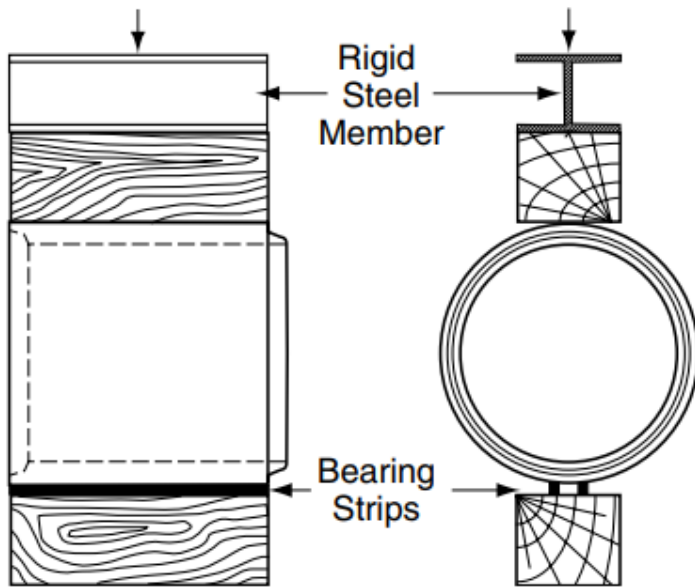
1930s – Marston-Spangler Model

Traditional Beddings – Class A, B, C, D
 Indirect Design Method only

1980s – Heger Pressure Distribution

Standard Installation Beddings – Type 1, 2, 3, 4
 Direct Design or Indirect Design Methods

3-EDGE BEARING TEST (D-LOAD TEST)



Criteria in ASTM C497:

- 0.01 in. design crack (D-Load)
- Ultimate strength



Dime is 0.053" thick
5 times the D-Load

RCP STRENGTH CLASSIFICATIONS

Example:

What is the minimum load required for a **18 inch Class V** pipe in a 3EB Test?

$$\begin{aligned} D_{0.01} &= \text{Strength} \times \text{Pipe length} \times \text{Inside Dia} \\ &= (3000 \text{ lbs/ft/ft})(8 \text{ ft})(1.5 \text{ ft}) \\ &= 36,000 \text{ lbs} \end{aligned}$$

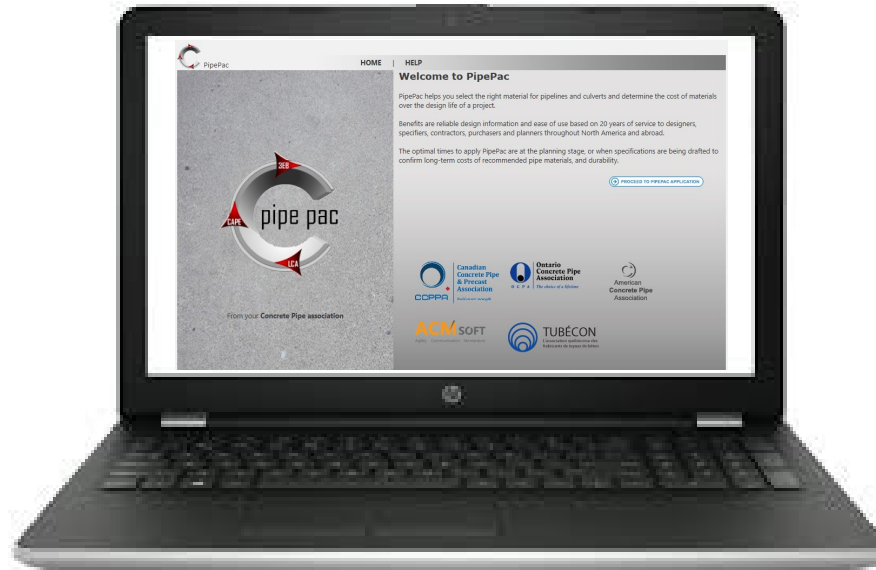
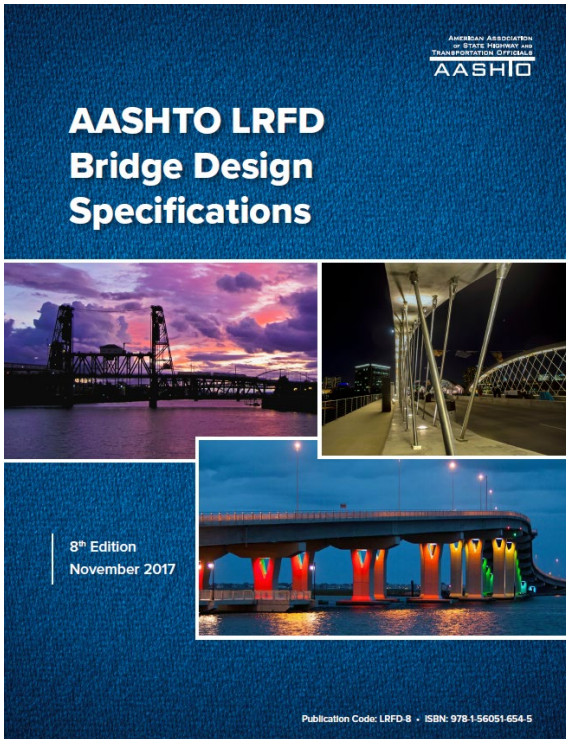
$$\begin{aligned} D_{ult} &= (3750 \text{ lbs/ft/ft})(8 \text{ ft})(1.5 \text{ ft}) \\ &= 45,000 \text{ lbs} \end{aligned}$$

ASTM C76	$D_{0.01}$ (lbs/ft/ft)	D_{ult} (lbs/ft/ft)
Class I	800	1200
Class II	1000	1500
Class III	1350	2000
Class IV	2000	3000
Class V	3000	3750

Reinforced Concrete Pipe Design

Indirect Design Method with Standard Installations

CONCRETE PIPE DESIGN OPTIONS



PipePac software

www.pipepac.com

Efficient, but understand design principles

FOR CONCRETE PIPE

LRFD FILL HEIGHT TABLES

Class I Class II Class III Class IV Class V Special Design

	10	11	12	13	14									
781	858	934	1011	1087										
786	841	915	990	1065										
761	835	909	983	1056										
763	836	909	983	1056										
768	841	915	988	1062										
769	842	915	989	1062										
772	845	919	992	1065										
777	850	923	996	1069										
783	856	929	1003	1076										
788	861	933	1006	1079										
795	867	940	1013	1085										
803	876	948	1021	1094										
813	885	958	1031	1103										
66	906	955	687	646	655	691	736	767	750	823	896	869	1041	1114
72	850	837	679	643	658	696	741	793	761	834	907	880	1053	1126
78	802	820	672	642	660	697	744	796	768	841	913	886	1059	1131
84	763	805	665	641	661	700	747	799	775	848	920	893	1065	1138
90	730	791	660	641	664	703	750	803	863	855	927	899	1072	1144
96	703	756	655	642	666	706	754	807	867	862	934	1006	1078	1151
102	679	734	662	649	674	714	761	814	875	937	941	1013	1086	1158
108	660	723	668	657	681	721	769	822	882	945	949	1021	1093	1165
114	643	729	675	665	689	729	776	830	890	952	1016	1028	1100	1172
120	629	734	682	670	697	737	784	837	898	960	1024	1036	1108	1180
126	617	740	689	678	705	744	792	845	905	968	1032	1047	1119	1191
132	607	745	691	686	712	752	800	853	913	976	1039	1056	1128	1200
138	599	751	686	694	720	760	808	861	921	983	1047	1112	1178	1250
144	592	757	692	701	728	768	816	869	929	991	1055	1120	1186	1253

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First Principles
Accurate, but tedious

Fill Height Tables
Quick, but understand the assumptions used

INDIRECT DESIGN OVERVIEW

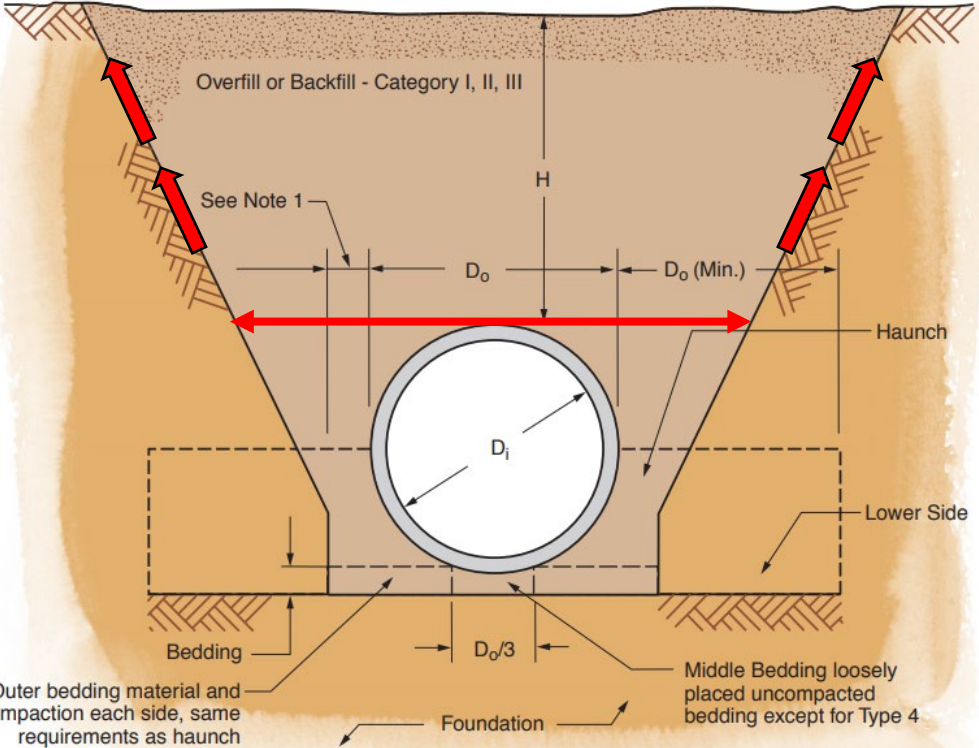
$$D_{0.01} = \left(\frac{W_E + W_F}{B_{FE}} + \frac{W_L}{B_{FLL}} \right) \left(\frac{FS}{Dia} \right)$$

See **ACPA Design Data 9**
Standard Installations and
Bedding Factors for the Indirect
Design Method

- Determine all loads – Earth (W_E), Live (W_L), Fluid (W_F), Surcharge
- Select a Standard Installation bedding type
- Determine Bedding Factors (B_{FE} & B_{FLL})
- Apply a Factor of Safety (FS) = 1.0 for $D_{0.01}$
- Calculate D-Load to produce 0.01” crack ($D_{0.01}$ in lb/ft/ft)
- Select a standard pipe strength class

RCP INSTALLATION TYPES

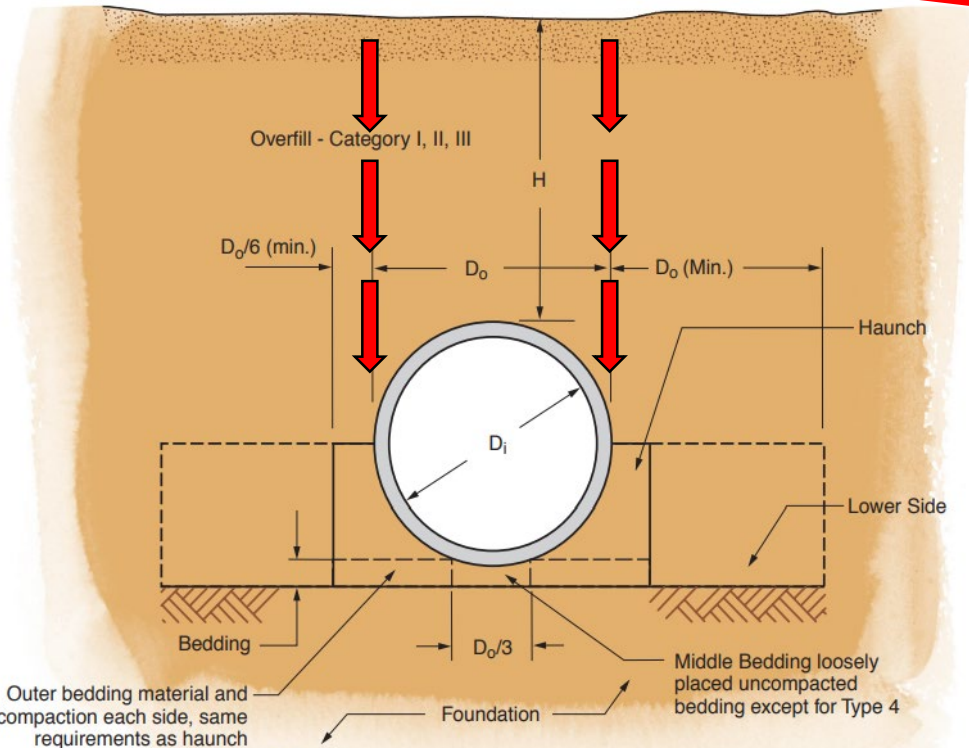
Assume the Worst-Case
Use **positive projection**
embankment for design



Note 1: Clearance between pipe and trench wall shall be adequate to enable specific compaction, but not less than $D_o/6$.

Trench Installation

Upward friction from trench walls
reduces the earth load



Embankment Installation

Drag down friction from side soil
increases the earth load

WEIGHT OF THE PIPE

$$A \text{ wall} = \frac{D_i}{12}$$

$$B \text{ wall} = \frac{D_i}{12} + 1$$

$$C \text{ wall} = \frac{D_i}{12} + 1.75$$

Where:

D_i = inside diameter in inches

- Concrete pipe wall thickness may vary by producer

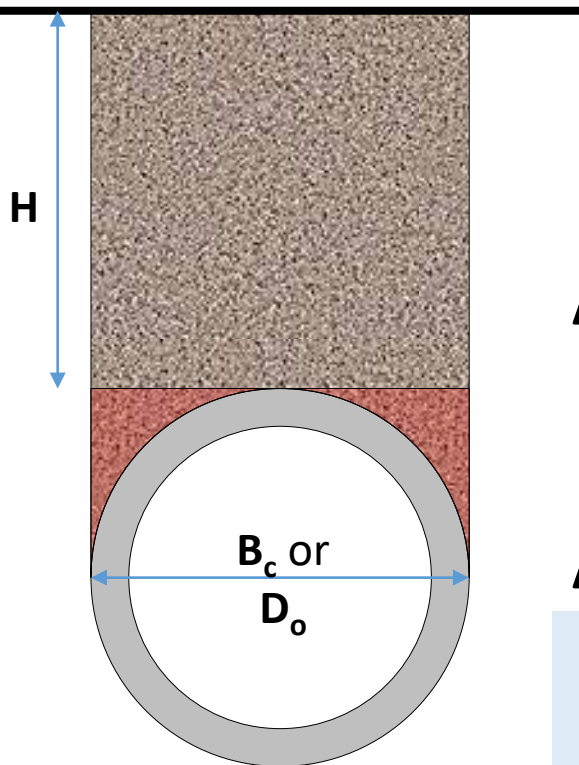
Direct Design – must consider pipe self-weight

Indirect Design – pipe self-weight is ignored since already accounted for in the 3EB Test

EARTH LOAD (W_E)

$$D_{0.01} = \left(\frac{W_E + W_F}{B_{FE}} + \frac{W_L}{B_{FLL}} \right) \left(\frac{FS}{Dia} \right)$$

$W_E = \text{Vertical Arching Factor (VAF)} \times \text{Prism Load (PL)}$



AASHTO (12.10.2.1-1):

$$W_E = F_e w B_c H$$

VAF

ACPA (Design Data 9):

$$W_E = \text{VAF} \cdot w \left[H + \frac{D_o(4 - \pi)}{8} \right] D_o$$

AASHTO 12.10.2.1:

Unit weight of soil (w) cannot be $< 110 \text{ lb/ft}^3$.

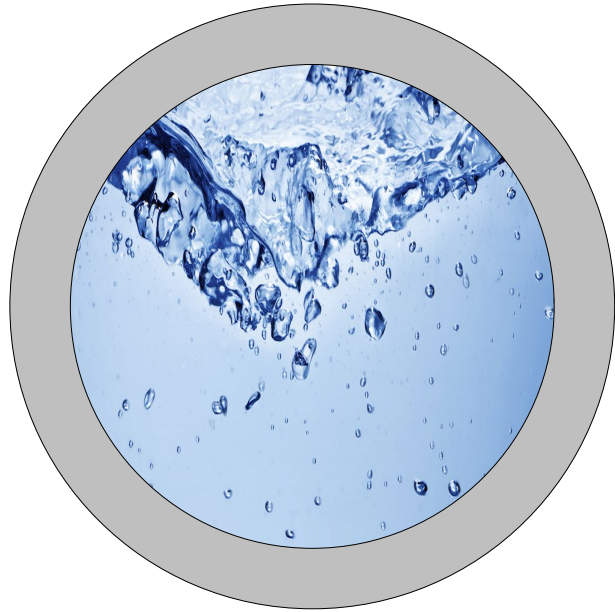
Typically **120 lb/ft³** used

VAF for Embankment:

Standard Installation	VAF
Type 1	1.35
Type 2	1.40
Type 3	1.40
Type 4	1.45

FLUID LOAD (W_F)

$$D_{0.01} = \left(\frac{W_E + W_F}{B_{FE}} + \frac{W_L}{B_{FLL}} \right) \left(\frac{FS}{Dia} \right)$$



AASHTO 12.10.2.2: Weight of fluid inside the pipe must be considered in design

- Fluid Load is assumed to be supported by lower part of the pipe (like earth load)


$$W_F = \gamma_w \cdot \pi \left(\frac{D_i}{24} \right)^2$$

Where:

D_i = inside diameter in inches

γ_w = unit weight of water = 62.4 lb/ft³

LIVE LOAD (W_L)

$$D_{0.01} = \left(\frac{W_E + W_F}{B_{FE}} + \frac{W_L}{B_{FLL}} \right) \left(\frac{FS}{Dia} \right)$$


AASHTO 3.6.1.2.6a: For single span culverts – live load (truck) is negligible when depth of fill is greater than 8 ft and exceeds the span.

Highway Loads – ACPA Design Data 1

Aircraft Loads – ACPA Design Data 2

Railroad Loads – ACPA Design Data 3

BEDDING FACTORS (B_f)

B_f = ratio of max. moments in pipe wall:

$$B_f = \frac{M_{\text{Test}}}{M_{\text{Field}}}$$



$$M_{\text{Test}} = B_f \cdot M_{\text{Field}}$$

$$D_{0.01} = \left(\frac{W_E + W_F}{B_{FE}} + \frac{W_L}{B_{FLL}} \right) \left(\frac{FS}{\text{Dia}} \right)$$

Embankment Earth Load Bedding Factors (B_{FE}):

Pipe Dia (in.)	Standard Installation			
	Type 1	Type 2	Type 3	Type 4
12	4.4	3.2	2.5	1.7
24	4.2	3.0	2.4	1.7
36	4.0	2.9	2.3	1.7
72	3.8	2.8	2.2	1.7
144	3.6	2.8	2.2	1.7

Live Load Bedding Factors (B_{FLL}):

Pipe Dia (in.)	Fill Height (ft.)	
	< 2.0 ft	≥ 2.0 ft
12	3.2	2.4
18	3.2	2.4
24	3.2	2.4
30 and larger	2.2	2.2

Note: These B_{FLL} in LRFD (8TH Ed) is not the same as the 7th Ed or the ACPA DD9.

ACPA LRFD FILL HEIGHT TABLES



- Based on **Indirect Design** as per LRFD Bridge Design Specification (7TH Ed)
- **Positive Projecting Embankment**
- **C wall** for all sizes >> max. prism load
- Soil unit weight = **120 lb/ft³**
- AASHTO **HL-93** live load
- For Type 1: D-Loads increased by multiplying installation factor of **1.10** (AASHTO 12.10.4.3.1)

Plastic Pipe Design

PLASTIC PIPE DESIGN METHOD

12.12 Thermoplastic Pipes

Strength Limit States:

- Thrust
- Buckling
- Combined strains

Service Limit States:

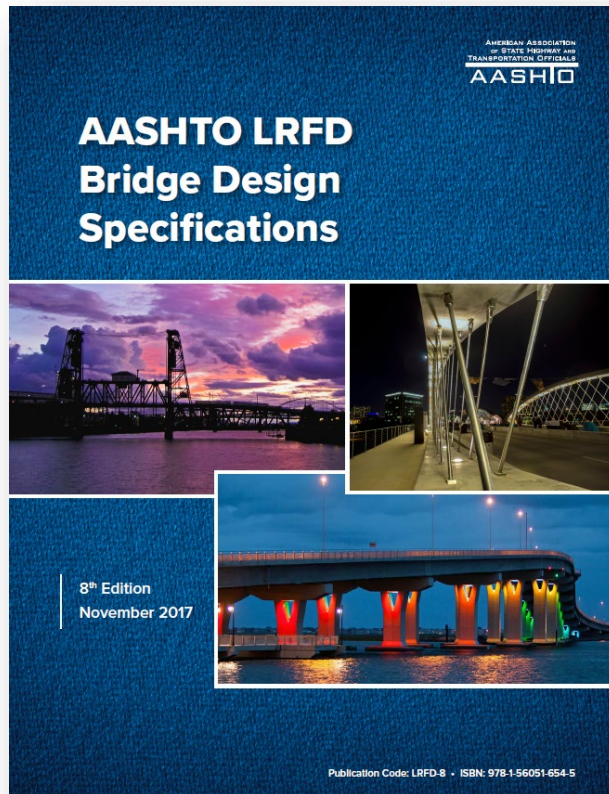
- Deflection

Also, check flotation

AASHTO LRFD assumes that native soil is stiff and ignores the transfer of load to the in-situ trench walls.

Commentary C12.12.3.5:

The width of structural backfill is an important consideration when the in situ soil in the trench wall or the embankment fill at the side of the structural backfill is soft. Currently, only AWWA Manual M45, The Fiberglass Pipe Design Manual, addresses this issue.



FILL HEIGHT TABLES

Common assumptions used in plastic pipe fill height tables:

- Pipe is installed in accordance with **ASTM D2321**
- Water table is below the pipe (**no hydrostatic pressure**)
- Native soil is **very stiff**

Example: 48 in. HDPE pipe with
Class 2 backfill compacted to 95%

Maximum Cover			
JM Eagle Eagle Corr PE (Dual Wall)	Prinsco GoldFlo (Dual Wall)	Haviland Smooth Flow (Dual Wall)	ADS N-12 (AASHTO)
30 ft	24 ft	22 ft	17 ft

PLASTIC PIPE PROPERTIES

- Pipe performance depends on profile wall geometry which vary significantly
 - Moment of inertia (I)
 - Radius to centroid of pipe profile (R)
 - Spacing of corrugations (ω)
 - Wall area (A_g) and effective wall area (A_{eff})
- Short and long-term mechanical properties vary by type of plastic pipe
 - See LRFD [Table 12.12.3.3-1](#)



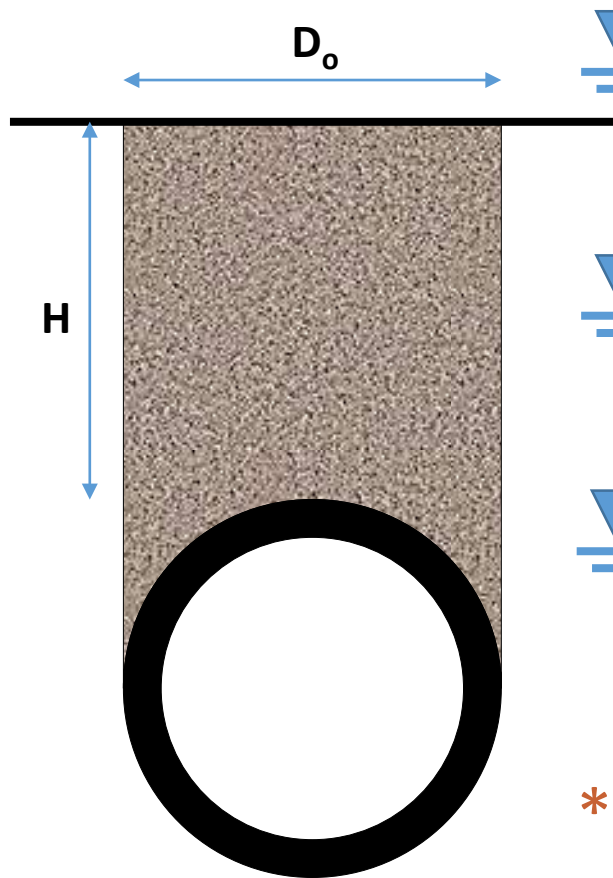
Source: NCHRP Report 631

C12.12.3.2

Historically, AASHTO bridge specifications have contained minimum values for the moment of inertia and wall area of thermoplastic pipe; however, these values have been minimum values and are not meaningful for design. This is particularly so since provisions to evaluate local buckling were introduced in 2001. These provisions require detailed profile geometry that varies with manufacturer. Thus, there is no way to provide meaningful generic information on section properties. A convenient method for determining section properties for profile wall pipe is to make optical scans of pipe wall cross-sections and determine the properties with a computer drafting program.

SOIL PRISM PRESSURE (P_{sp})

P_{sp} is calculated for 3 possible conditions:



1. Water table above top of pipe and at or above the ground surface

$$P_{sp} = \frac{\left(H + 0.11 \frac{D_o}{12} \right) \gamma_b}{144}$$

2. Water table above top of pipe and below the ground surface

$$P_{sp} = \frac{1}{144} \left[\left[\left(H_w - \frac{D_o}{24} \right) + 0.11 \frac{D_o}{12} \right] \gamma_b + \left[H - \left(H_w - \frac{D_o}{24} \right) \right] \gamma_s \right]$$

3. Water table below top of pipe

$$P_{sp} = \frac{\left(H + 0.11 \frac{D_o}{12} \right) \gamma_s}{144}$$

Also check for FLOTATION

*Evaluate multiple conditions if water table fluctuates.

THRUST

$$\epsilon_{uc} \leq \Phi_T \epsilon_{yc}$$

Factored compressive strain

Factored compressive strain limit

$$\epsilon_{uc} = \frac{T_u}{1000(A_{eff}E_p)}$$

Factored thrust

$$T_u = \left[\eta_{EV} (\gamma_{EV} K_{\gamma E} K_2 VAF P_{sp} + \gamma_{WA} P_w) + \eta_{LL} \gamma_{LL} P_L C_L F_1 F_2 \right] \frac{D_o}{2} \quad (12.12.3.5-1)$$

Soil Load (reduced by VAF)

Groundwater

Live Load

in which:

$$VAF = 0.76 - 0.71 \left(\frac{S_H - 1.17}{S_H + 2.92} \right) \quad (12.12.3.5-3)$$

$$S_H = \frac{\phi_s M_s R}{E_p A_g} \quad (12.12.3.5-4)$$

$$C_L = \frac{L_w}{D_o} \leq 1.0 \quad (12.12.3.5-5)$$

$$F_1 = \frac{0.75 D_o}{L_w} \geq F_{min} \quad (12.12.3.5-6)$$

$$F_{min} = \frac{15}{D_i} \geq 1 \quad (12.12.3.5-7)$$

$$F_2 = \frac{0.95}{1 + 0.6 S_H} \quad (12.12.3.5-8)$$

- Check both **springline** & **crown** of pipe
- Total load contributes – **soil load**, **live load** & **hydrostatic load**
- Short & long-term material properties need to be evaluated due to time-dependent nature of plastic pipe

BUCKLING

- Pipe wall must have sufficient stiffness to remain stable under compression loads.

$$\epsilon_{uc} \leq \Phi_{bck} \epsilon_{bck}$$

Factored compressive strain

Resistance factor = 0.7

Buckling strain capacity of pipe

Poor soil support decreases pipe's ability to resist buckling

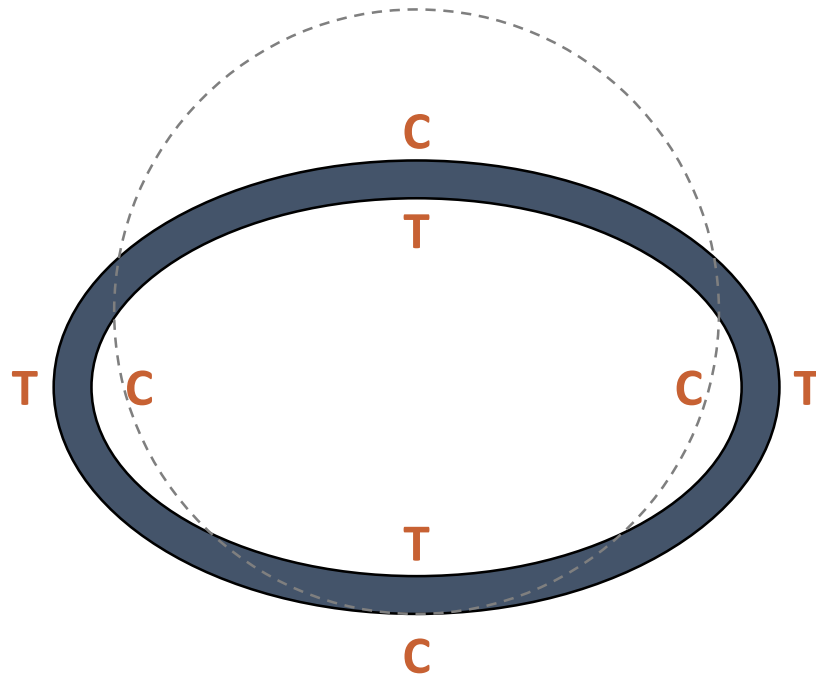
$$\epsilon_{bck} = \frac{1.2C_n (E_p I_p)^{\frac{1}{3}}}{A_{eff} E_p} \left[\frac{\phi_s M_s (1-2\nu)}{(1-\nu)^2} \right]^{\frac{2}{3}} R_h \quad (12.12.3.10.1e-2)$$

in which:

$$R_h = \frac{11.4}{11 + \frac{D}{12H}} \quad (12.12.3.10.1e-3)$$

COMBINED STRAINS

- Must check combined strains at extreme fibers since bending strain from deflection creates **tension (T)** and **compression (C)** zones



12.12.3.10.2b—Combined Strain

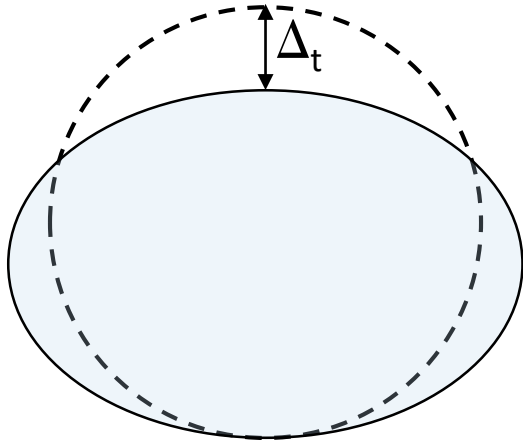
If summation of axial strain, ϵ_{uc} , and bending strain, ϵ_f , produces tensile strain in the pipe wall, the combined strain at the extreme fiber where flexure causes **tension** shall satisfy:

$$\epsilon_f - \epsilon_{uc} < \phi_f \epsilon_{yt} \quad (12.12.3.10.2b-1)$$

The combined strain at the extreme fiber where flexure causes **compression** shall satisfy:

$$\epsilon_f + \epsilon_{uc} < \phi_T (1.5\epsilon_{yc}) \quad (12.12.3.10.2b-2)$$

DEFLECTION



$$\Delta_t = \frac{K_B (D_L P_{sp} + C_L P_L) D_o}{1000 \left(\frac{E_p I_p}{R^3} + 0.061 M_s \right)} + \epsilon_{sc} D$$

Soil Load

Live Load

Circumferential Shortening

Pipe Stiffness

Soil Stiffness

- Caused by **bending deformation** plus **circumferential shortening** due to thrust
- Controlled by proper soil support and must be verified with a **deflection test**
- Maximum allowable deflection = **5.0%**

SECANT CONSTRAINED SOIL MODULUS (M_s)

- All backfill soils are combined into three broad groups
 - **Sn** – sands and gravels
 - **Si** – silts
 - **Cl** – clays
- More useful than E' soil stiffness for deep installations since M_s increases with depth

Table 12.12.3.5-1— M_s Based on Soil Type and Compaction Condition

P_{sp} Stress Level (psi)	Sn-100 (ksi)	Sn-95 (ksi)	Sn-90 (ksi)	Sn-85 (ksi)
1.0	2.350	2.000	1.275	0.470
5.0	3.450	2.600	1.500	0.520
10.0	4.200	3.000	1.625	0.570
20.0	5.500	3.450	1.800	0.650
40.0	7.500	4.250	2.100	0.825
60.0	9.300	5.000	2.500	1.000
P_{sp} Stress Level (psi)		Si-95 (ksi)	Si-90 (ksi)	Si-85 (ksi)
1.0		1.415	0.670	0.360
5.0		1.670	0.740	0.390
10.0		1.770	0.750	0.400
20.0		1.880	0.790	0.430
40.0		2.090	0.900	0.510
60.0				
P_{sp} Stress Level (psi)		Cl-95 (ksi)	Cl-90 (ksi)	Cl-85 (ksi)
1.0		0.530	0.255	0.130
5.0		0.625	0.320	0.175
10.0		0.690	0.355	0.200
20.0		0.740	0.395	0.230
40.0		0.815	0.460	0.285
60.0		0.895	0.525	0.345

Plastic pipe is extremely
INSTALLATION SENSITIVE!

EMBEDMENT SOIL & DEFLECTION

Given: $D_i = 48$ in. $H = 25$ ft $P_w = 0$ psi
 $D_o = 54.26$ in. $K_B = 0.1$ $A_g = 0.441$ in²/in
 $R = 25.27$ in. $D_L = 1.5$ $A_{eff} = 0.305$ in²/in
 $E_{pi} = 110$ ksi $C_L = 1.0$
 $E_{P75} = 21$ ksi $P_{sp} = 21.2$ psi
 $I_p = 0.65$ in⁴/in $P_L = 0.336$ psi

$$\Delta_t = \frac{K_B (D_L P_{sp} + C_L P_L) D_o}{1000 \left(\frac{E_p I_p}{R^3} + 0.061 M_s \right)} + \epsilon_{sc} D$$

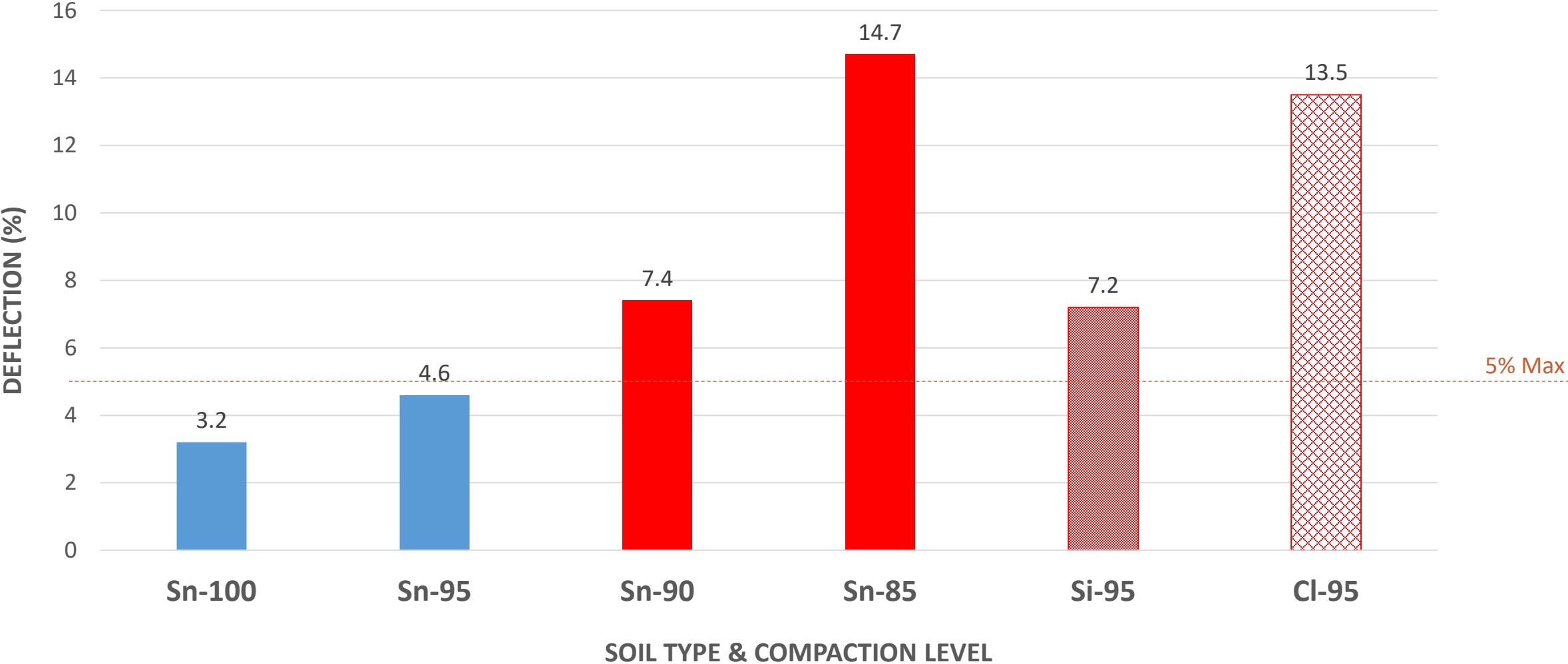
Various soils @ 95% compaction:

Soil Type & Compaction	M _s	Deflection
Sn-95	3.50	4.6 %
Si-95	1.89	7.2 %
Cl-95	0.75	13.5 %

Sn soil with various compaction:

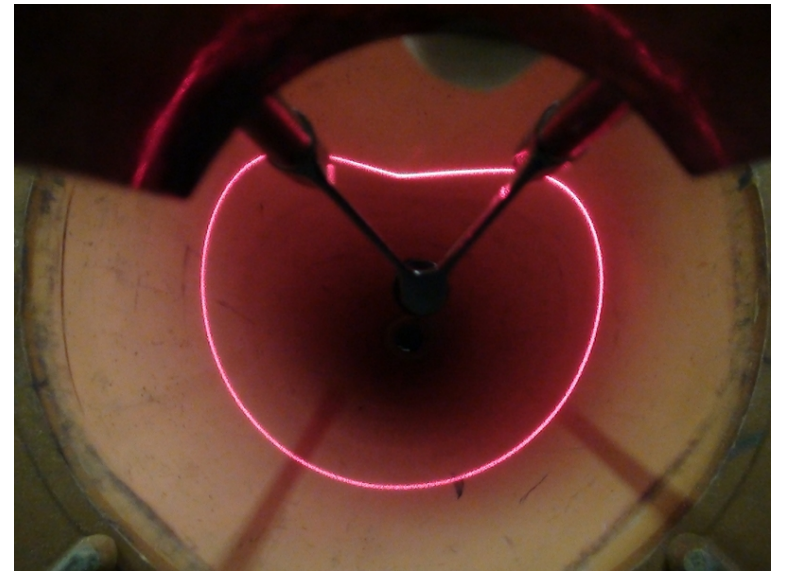
Soil Type & Compaction	M _s	Deflection
Sn-100	5.63	3.2 %
Sn-95	3.50	4.6 %
Sn-90	1.82	7.4 %
Sn-85	0.66	14.7 %

EMBEDMENT SOIL & DEFLECTION



DEFLECTION TESTING

- Plastic pipe requires a deflection test to verify proper soil embedment
- Frequency of deflection tests:
 - No sooner than **30 days after backfill** – AASHTO Section 30
 - Prior to final acceptance or end of warranty
 - As part of on-going pipe maintenance
- Plastic pipe products have different ***Base Inside Diameters***



Load Lag, Deflection Lag, and Time Lag

Amster Howard

TECH NOTE: Supplement to Pipeline Installation

“... the maximum load on a pipe does not occur until three to six months after backfilling...”

PLASTIC PIPE DESIGN METHOD SUMMARY

12.12 Thermoplastic Pipes

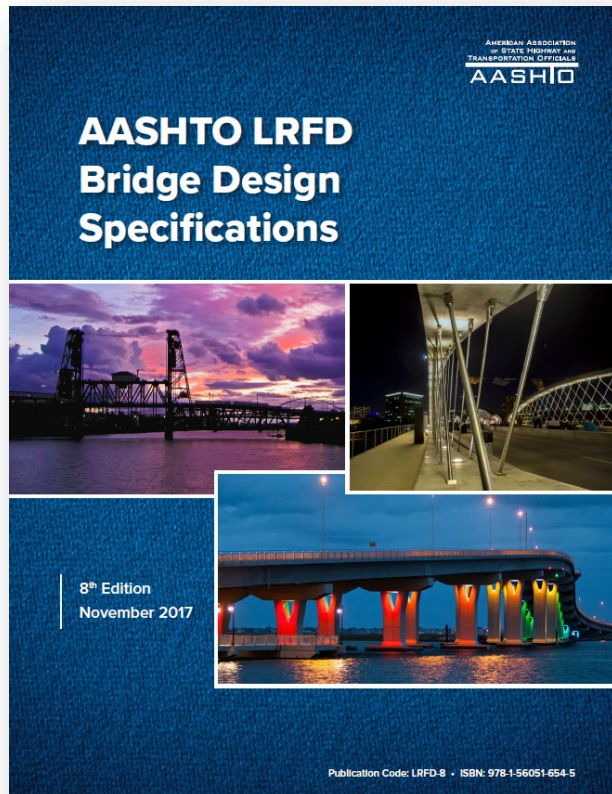
Strength Limit States:

- Thrust – *Compressive limits of the pipe material*
- Buckling – *Dependant on both soil and pipe properties*
- Combined strains – *Material limits with deflection strains added*

Service Limit States:

- Deflection – *Installation sensitive, verify with deflection test.*

Also, check flotation



FUNDAMENTAL DIFFERENCES IN DESIGN

RIGID CONCRETE PIPE

- Standard strength classes
- Indirect or Direct Design
- Primary structure is pipe (60-75%)
- Structure built & tested at plant with 3EB test
- Design life based on historical performance data
- Design software available

FLEXIBLE PLASTIC PIPE

- Wide range of pipe products/profiles
- Direct design only
- Primary structure is soil (50-90%)
- Structure built & tested in field with deflection test
- Design life based on time-dependent behavior of material



THANK YOU